



The Fibonacci Quarterly

THE OFFICIAL JOURNAL OF THE FIBONACCI ASSOCIATION

TABLE OF CONTENTS

Fibonacci Conference and Caen Proceedings Announcements	2
Further Closed Forms for Finite Sums of Weighted Products of Generalized Fibonacci Numbers	<i>R. S. Melham</i> 3
Polynomial Extensions of a Diminnie Delight Revisited: Part II	<i>Thomas Koshy and Zhenguang Gao</i> 10
Conditional (Strong) Divisibility Sequences	<i>Murat Sahin and Elif Tan</i> 18
Congruences Modulo 5 for Partitions Into at Most Four Parts	<i>Michael D. Hirschhorn</i> 32
Further Closed Forms for Finite Sums of Weighted Products of the Sine and Cosine Functions	<i>R. S. Melham</i> 38
Donald Dines Wall's Conjecture	<i>Jiří Kláška</i> 43
On X -Coordinates of Pell Equations that Are Repdigits	<i>Bernadette Faye and Florian Luca</i> 52
On the $D(4)$ -Diophantine Triples of Fibonacci Numbers	<i>Salah Eddine Rihane, Mohand Ouamar Hernane, and Alain Togbé</i> 63
A Formula for an Infinite Family of Fibonacci-Word Sequences	<i>Martin Griffiths</i> 75
Elementary Problems and Solutions	<i>Edited by Harris Kwong</i> 81
Advanced Problems and Solutions	<i>Edited by Florian Luca</i> 89
Paul Bruckman Prize	96

Journal for Research in Mathematics Education

EDITORIAL

-
- The Role of Replication Studies in Educational Research** 2
Jinfa Cai, Anne Morris, Charles Hohensee, Stephen Hwang,
Victoria Robison, and James Hiebert

ARTICLES

-
- Three Conceptual Replication Studies in Group Theory** 9
Kathleen Melhuish
- Brief Report: The Effects of Preservice Elementary School Teachers' Accurate Self-Assessments in the Context of Whole Number** 39
Eva Thanheiser
- Exploring Longitudinal Changes in Teacher Expectancy Effects on Children's Mathematics Achievement** 57
Faiza M. Jamil, Ross A. Larsen, and Bridget K. Hamre

RESEARCH COMMENTARIES

-
- On Replications** 91
Alan H. Schoenfeld
- When and Why Replication Studies Should Be Published: Guidelines for Mathematics Education Journals** 98
Jon R. Star
- Rejoinder: Reframing Replication Studies as Studies of Generalizability: A Response to Critiques of the Nature and Necessity of Replication** 104
Kathleen Melhuish and Eva Thanheiser
- Rejoinder: A Reflection on the Evolution of a Replication Study** 111
Faiza M. Jamil

Journal for Research in Mathematics Education

EDITORIAL

- Data in a Brave New World: Reducing Isolation to Amplify the Impact of Educational Research on Practice** 118
Jinfa Cai, Anne Morris, Charles Hohensee, Stephen Hwang, Victoria Robison, and James Hiebert

RESEARCH COMMENTARY

- Theorizing Collaborative Mathematics Teacher Learning in Communities of Practice** 125
Nicole A. Bannister

ARTICLES

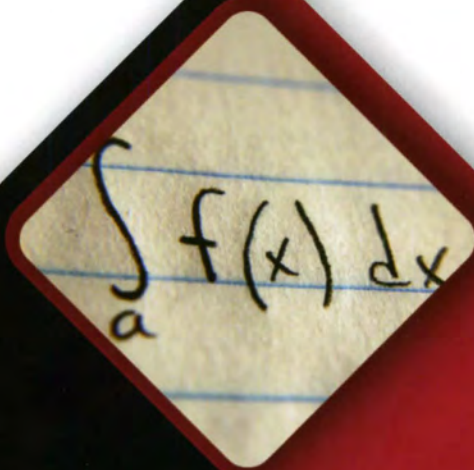
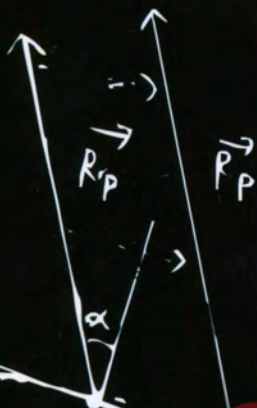
- Equity Analytics: A Methodological Approach for Quantifying Participation Patterns in Mathematics Classroom Discourse** 140
Daniel L. Reinholz and Niral Shah
- Loving and Loathing: Portrayals of School Mathematics in Young Adult Fiction** 178
Lisa Darragh
- Brief Report: A Progression of Fraction Schemes Common to Chinese and U.S. Students** 210
Anderson Norton, Jesse L. M. Wilkins, and Cong ze Xu

BOOK REVIEWS

- A Guide to Analyzing Mathematics Tasks and Their Implementation in Curriculum Resources** 228
Janine T. Remillard, Michael Manganello, and Amber Daniel
- A Review of Cases for Mathematics Teacher Educators: Facilitating Conversations About Inequities in Mathematics Classrooms** 232
Nicole M. Joseph, Christopher C. Jett, and Jacqueline Leonard

L

OSANGES



SBPMEF

N° 39
DÉCEMBRE 2017



Losanges

N°39 Décembre 2017₂

Éditorial, *V. Henry*



Réflexions

- ◆ Le mystère des sangaku, *B. Honclaire* 3
- ◆ Les élèves et le cours d'analyse, *M. Cornez* 8
- ◆ Sensibiliser aux probabilités, *G. Noël et J.-M. Desbonnez* 18
- ◆ Sur les empilements infinis..., *P. Lecomte* 30
- ◆ Une curiosité, *M. Cornez* 38
- ◆ Triangles inscrits d'aire maximale, *T. Libert* 40
- ◆ Problèmes d'arpenteurs, *P. Lapôtre* 44
- ◆ Grands nombres..., *M. Seville* 48



Technologies

- ◆ Mathématiques et smiley, *J.-M. Desbonnez* 51



Jeux et concours

- ◆ EGMO 2017, *P.-A. Jacqmin et M. Seville* 54
- ◆ Mat croisé 38 : solution, *J.-M. Desbonnez* 60
- ◆ Mat croisé, *J.-M. Desbonnez* 61
- ◆ Problèmes, *M. Seville* 62



Regards sur ...

- ◆ ... le Stomachion d'Archimède, *G. Noël* 65
- ◆ ... des livres, *J. Miewis* 67
- ◆ ... un mathématicien aux métallos, *J.-M. Desbonnez* 69
- ◆ ... les JN de l'APMEP, *V. Henry et M.-F. Guissard* 70

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Focus Issue

Productive Struggle



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FEATURES

194 **Productive Struggle for All:
Differentiated Instruction**
*Sararose D. Lynch, Jessica H. Hunt,
and Katherine E. Lewis*
Consider strategies that create access
while maintaining the cognitive demand
of a mathematics task.

202 **Scaffolding for Access to
Productive Struggle**
*Angela T. Barlow, Natasha E. Gerstenschlager,
Jeremy F. Strayer, Alyson E. Lischka,
D. Christopher Stephens, Kristin S. Hartland,
and J. Christopher Willingham*
Examining two lessons using the same
problem illuminates a way that scaffolding
can support access to productive struggle.

208 **Seven Billion People:
Fostering Productive Struggle**
Jaclyn M. Murawska
A cognitively demanding real-world task
can help shape students' mathematical
dispositions.

216 **Supporting All Learners in
Productive Struggle**
*Cynthia Townsend, David Slavit,
and Amy Roth McDuffie*
To support a growth mindset in students,
consider components involving cognitive,
social, and emotional aspects so that
students can work within their zone of
productive struggle.



202



216



208

DEPARTMENTS

- 181** *Mathematics Teaching in the Middle School Online*
- 183** *By Way of Introduction*
Productive Struggle
Clayton Edwards
- 184** *Solve It Student Thinking*
Shapes and Sizes
Annie Perkins and Pamela J. Wells
- 188** *Cartoon Corner*
Snow Day
Hoyun Cho, Katie A. Hendrickson, and Rhonda Birnie
- 192** *Palette of Problems*
Stephan Pelikan, Anna F. DeJarnette, and Stephen Phelps
- 226** *Quick Reads*
Using Tools to Make Sense of Right Triangles
Terri L. Kurz and Mi Yeon Lee
- 231** *Mathematical Explorations*
The Mathematics of Loopy Picture Frames
Madhavi Vishnubhotla and Mika Munakata
- 236** *Window on Resources*
- 240** *Math for Real*
Added Sugar Intake
Christy Danko Graybeal



184



looking ahead in *MTMS* to March

- “Dancing Our Way to Geometric Transformations,” by Alison E. Leonard and Nicole A. Bannister
- “Assembling the Puzzle of Mathematical Strengths,” by Dorothy Y. White, Carlos Nicolas Gomez, Fredric Rushing, Nicholas Hussain, Kristina Patel, and Jason Pratt
- “Developing Communication and Metacognition through Question Generation,” by Kate Raymond, Melissa Gunter, and Kansas Conrady

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"Translation, rotation, reflection..."

DANCING TO Geometry

- SUPPORTING THINKERS p.268
- DEVELOPING METACOGNITION p.276

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FEATURES

258 **Dancing Our Way to Geometric Transformations**

Alison E. Leonard and Nicole A. Bannister

Students slide into reflections, rotations, and translations and take giant leaps forward in their geometric understanding.

268 **Assembling the Puzzle of Mathematical Strengths**

Dorothy Y. White, Carlos Nicolas Gomez, Fred Rushing, Nicholas Hussain, Kristina Patel, and Jason Pratt

A professional learning community, or PLC, identifies students' mathematical strengths and shows how the PLC uses the information to support students as mathematical thinkers and doers.

276 **Developing Communication and Metacognition through Question Generating**

Kate Raymond, Melissa Gunter, and Kansas Conrady

The strategy of question generating can be used to develop communication and metacognitive skills in students, thus leading to more meaningful discourse.



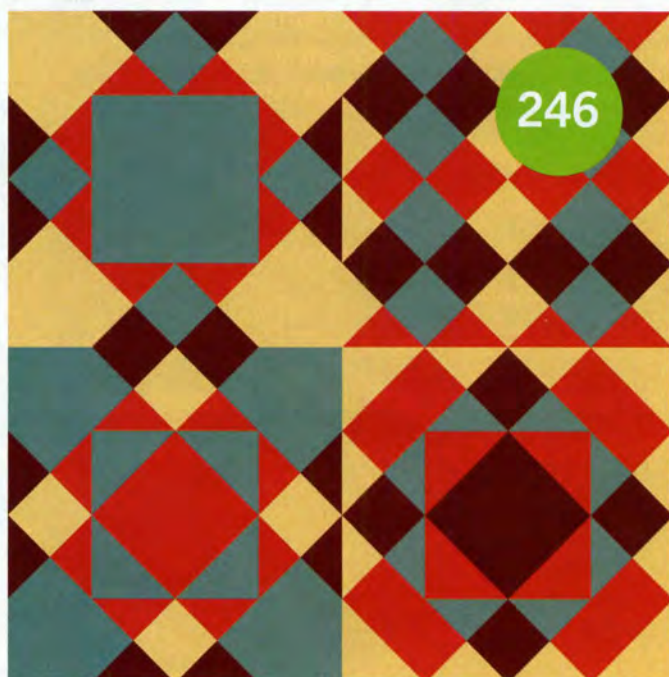
DEPARTMENTS

- 245** *Mathematics Teaching in the Middle School Online*
- 246** *Solve It*
Picturing Infinite Fraction Sums
Annie Perkins and Christy Pettis
- 248** *Solve It Student Thinking*
A Design with Disks
Annie Perkins and Pamela J. Wells
- 252** *Cartoon Corner*
Taxing Problems
Joanne Caniglia, Michelle Meadows, Hoyun Cho, David B. Spangler, and Katie A. Hendrickson
- 256** *Palette of Problems*
Stephan Pelikan, Anna F. DeJarnette, and Stephen Phelps
- 284** *Quick Reads*
Strengthening Partnerships through Family Math Nights
Lynn Liao Hodge and Michael Lawson
- 288** *Mathematical Explorations*
Abacus Interactive
Ellen Robinson, Xiaowen Cui, Nama Namakshi, Hiroko K. Warshauer, Sonalee Bhattacharyya, and Christina Koehne
- 299** *Window on Resources*
- 304** *Math for Real*
Parking Lot Design Contest
Hyunyi Jung and Ji-Yeong I

304



246



looking ahead in *MTMS*

IN APRIL 2018

- “From Mathematical Reading to Mathematical Literacy,” by Gregory Beaudine
- “Examining Mistakes to Shift Student Thinking,” by James C. Willingham, Jeremy F. Strayer, Angela T. Barlow, and Alyson E. Lischka
- “Minecraft Comes to Math Class,” by Kimberly Moore

June 2017

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Volume 25, Number 2, June 2017

CONTENTS

- Prosenjit Sen, Alakes Maiti, and G. P. Samanta** 149
Dynamics of a Symbiotic Model with Herd Behaviour and Strong Allee Effect
- C. S. Kouzinopoulos, P. D. Michailidis, and K. G. Margaritis** 165
Parallel Two-Dimensional Pattern Matching Algorithms Based on GPU
- Claris Shoko, Delson Chikobvu, and Winston Garira** 181
Time-inhomogeneous Markov Modelling Of Hiv/aids Progression in South Africa
- Abhinandan Chowdhury and Mark Delcambre** 195
A Semi-Analytical Approach to Determine the Velocity Potential Around Two Spheres in Arbitrary Motion Through an Ideal Fluid
- Zvi Retchkiman Konigsberg** 213
Modelling and Verification Analysis of the Biological Interaction Between Species via a First Order Logic Approach
- Denis Bosq and Delphine Blanke** 229
Detecting Change-Points for Poisson Processes with Functional Data
- Hassina Arroudj, Idir Arab, and Abdelnasser Dahmani** 251
Strongly Mixed Random Errors in Mann's Iteration Algorithm for a Contractive Real Function
- George A. Anastassiou** 263
Arc tangent Function Based Banach Space Valued Neural Network Approximation
- Pradeep G** 295
The Conve
Diffusion I

4115

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Neural, Parallel & Scientific Computations

Volume 25, Number 3 & 4, September and December 2017

CONTENTS

- Vasilios Alexiades, Mustafa Zeki Elmas, and Gladys Alexandre** 307
Band formation in bacterial aerotaxis
- Mohd Younus Bhat** 313
Wavelet packets with their Fourier properties on local fields of prime characteristic
- Mitra Devkota and Gary Hatfield** 325
Spatial modeling techniques for Lattice Data
- Frederique Drullion** 335
Growth of groups of wind generated waves
- M. Z. Elmas, T. Mukherjee, G. Alexandre, and V. Alexiades** 345
A two pathways model for chemotactic signaling in *Azospirillum Brasilense*
- Basu Dev Ghimire and Ram Prasad Ghimire** 359
Reliability and availability of machines with two types of failures operated under periodic surveillance test
- Ram Ghimire, Samir Shrestha, Oliver Tse, and Shyam Sundar Sah** 375
Transient analysis of Markovian queue with flexible servers balking
- Sushil Ghimire, Gyan Bahadur Thapa, and Ram Prasad Ghimire** 385
Finite capacity M/M/r/N queueing model with additional servers
- Dadang Hamzah, Johan Tuwankotta, and Yudi Soeharyadi** 395
On the numerical solution of Fisher's equation by iterative operator-splitting method
- Mark M** 4115
Modelin
and an ex
- Ashok M** 417
Modelin
- Shiv Pr** 435
Stability

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SISAC 1061-5369(20170901)25:3/4;1-3

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Nº 182



ASÍ SON LAS TENDENCIAS DEL FUTURO

Inteligencia Artificial, Blockchain,
Internet de las Cosas, 5G,
Conducción autónoma...



**LLEVA TUS
CUENTAS AL DÍA**
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la economía familiar

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FOTOGRAFICOS
MÁS COMUNES**
Y cómo solucionarlos



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• Google
Pixel 2 y 2XL



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para preparar la
Navidad**

PRÁCTICOS

- Mejora la privacidad de **Windows 10**
- Saca todo el partido a **Amazon Prime Video**
- Da valor a tu perfil con **LinkedIn Pulse**

Sumario

Actualidad

- 06 Tecno-Flash**
- 08 Noticias y nuevos productos**
- 20 Sabías que...**
- 22 Magazine**
AWS: en manos de la nube
- 26 Tenemos correo**
- 27 El pasatiempo del mes**
- 28 TEMA DE PORTADA**
"Tecno" tendencias 2018

Hardware

- 38 Magazine**
Los 10 peores errores
fotográficos
- 42 Análisis de productos**
 - 42 Google Pixel 2 y 2 XL
 - 44 iPhone X
 - 46 Xbox One X
 - 47 Canon EOS 200D + EF-S 18-55
 - 48 Garmin VIRB 360
 - 49 Sphero Mini
 - 49 Kindle Oasis 2017
- 50 Guía de compras**
Tarjetas para grabar vídeo 4K
- 54 Gadget**
Acer Pawbo+
- 56 Accesorios**
Para los deportistas

Software

- 58 Seguridad**
BlueBorne: ¡a la captura!
- 60 Alternativas gratuitas para...**
Descargar música
- 62 Magazine**
8 Apps para celebrar la Navidad



28
"Tecno" tendencias
La tecnología que llegará el próximo año



22
Reportaje
Amazon Web Services: en manos de la nube



44
Hardware
Análisis a fondo del iPhone X



62
Software
Apps para celebrar la Navidad

Internet

- 66 Magazine**
Comunicaciones a través del mar
- 70 Magazine**
Haz más con tu router
- 72 Magazine**
Webs para ahorrar en la economía familiar
- 76 Enlaces**

Práctico SISTEMA

- 80 Windows**
Desactiva funciones de W10 y mejora tu privacidad
- 84 Windows**
Gestiona mejor el espacio en tu pantalla
- 86 Android**
Sincroniza tu móvil con Windows 10

DIGITAL MEDIA

- 88 Streaming**
Saca partido a Amazon Prime Video
- 92 Vídeo**
Edita tus vídeos con Story Remix

WEB

- 94 Redes sociales**
Publica artículos en LinkedIn Pulse
- 96 Seguridad**
Cómo compartir una cuenta sin revelar la contraseña
- 98 Aplicaciones**
Convierte tus correos en listas de tareas

- 102 Trucos**
- 106 Preguntas & Respuestas**
- 110 En 2 minutos**
- 112 Magazine**
Del walkie al smartphone

72 Internet

Lleva tus cuentas al día y empieza a ahorrar



80 Práctico

Desactiva funciones de Windows 10 para mejorar tu privacidad



88 Práctico

Saca todo el partido a Amazon Prime Video

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Recherches en didactique
des mathématiques

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Volume 37/2-3

LA PENSÉE SAUVAGE - ÉDITIONS

s o m m a i r e

sumario / summary

VIVIANE DURAND-GUERRIER, CÉCILE OUVRIER-BUFFET
Éditorial

151



MAHA ABBOUD, JANINE ROGALSKI
Des outils conceptuels pour analyser l'activité de l'enseignant
ordinaire utilisant des technologies en classe

161



BRITTA EYRICH JESSEN
How to generate autonomous questioning in secondary
mathematics teaching?

217



ÉDITH PETITFOUR
Outils théoriques d'analyse de l'action instrumentée,
au service de l'étude de difficultés d'élèves dyspraxiques
en géométrie

247



FRÉDÉRIK TEMPIER, CHRISTINE CHAMBRIS
Concevoir une ressource pour l'enseignement
de la numération décimale de position

289



FABRICE VANDEBROUCK, ALINE ROBERT
Activités mathématiques des élèves
avec les technologies numériques

333



NICOLAS BALACHEFF
Seymour PAPERT (1928-2016)
Aux sources d'une pensée innovante et engagée

383

37/2-3



9 782859 193232